Physical Model of Asteroid 1620 Geographos From Radar and Optical Data

R. S. Hudson

School of Electrical Engineering and Computer Science, Washington State University, Pullman

Washington 99164-2752

Phone: (509) 335-0922

Fax: (509) 335-3818

E-mail: hudson@eecs.wsu.edu

And

S. J. Ostro

Jet Propulsion Laboratory, California Institute of Technology, Pasadena, California 91109-8099

E-mail: ostro@echo.jpl.nasa.gov

Phone: (818) 354-3173

Fax: (818) 354-9476

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Please send all editorial correspondence to:

Scott Hudson

School of Electrical Engineering and Computer Science

Washington State University

Pullman Washington 99164-2752

E-mail: hudson@eecs.wsu.edu

Phone: (509) 335-0922

Fax: (509) 335-3818

We develop a physical model of asteroid 1620 Geographos using Goldstone delay-Doppler radar images obtained Aug. 1994 (Ostro *et al.* 1996, *Icarus* 121, 46-66) with resolution as fine as 75 m, and optical lightcurves obtained in 1969, 1983, and 1993-94 (Magnusson et al. 1996, *Icarus* 123, 227-244). The data set admits a geometric ambiguity that precludes a unique model. Within this constraint, our model has maximum extents of (5.0, 2.0, 2.1) \pm 0.15 km and volume of \leq 8.8 km³, equivalent to a sphere of \leq 2.56 km diameter. The radar equivalent spherical albedo is \geq 0.12. The photometric solution provides Hapke parameters $w \geq 0.22$, $g = -0.34 \pm 0.10$, and $\overline{\theta} = 25 \pm 10^\circ$ with assumed values h = 0.2 and $B_0 = 1.53$. The spin state solution does not differ significantly from that of Magnusson *et al.* having $\lambda = 55 \pm 4^\circ$, $\beta = -46 \pm 6^\circ$, and $P = 5.2233270 \pm 0.00000072$ hr. We identify seven main features in the delay-Doppler images and their corresponding locations on the model.

INTRODUCTION

The Earth-crossing asteroid (ECA) 1620 Geographos is interesting on several accounts. It is on the Minor Planet Center's list of Potentially Hazardous Asteroids (http://cfawww.harvard.edu/iau/lists/Dangerous.html). At about 5 km in maximum extent, it is one of the larger such objects. Lightcurves obtained in 1969 showed an amplitude of more than 2 magnitudes indicating a very elongated object (Magnusson et al. 1996). Radar observations during 1994 allowed unambiguous determination of the asteroid's pole-on silhouette and established it as the most elongated solar system object imaged to date (Ostro et al. 1995). Geographos was to have been the final target of the Clementine I spacecraft that would have made it the first ECA to be so visited. Unfortunately Clementine was unable to undertake that phase of its mission. So we are left with ground-based data to characterize this asteroid. In this paper we use the existing optical and radar data to form a physical model of Geographos.

The construction of a physical model from radar data has been demonstrated for the ECAs Castalia (Hudson and Ostro 1994) and Toutatis (Hudson and Ostro 1995). The models have been used to understand the asteroid's lightcurves, a process that also provided an independent test of the validity of the radar-derived models (Hudson *et al.* 1997, Hudson and Ostro 1998). As discussed below, with respect to physical modeling the Geographos radar data set has a geometric ambiguity not present in these other ECA radar data sets. In order to gain the maximum possible leverage over the shape, we have incorporated the optical data directly into the modeling process from the start.

DATA SET

The optical data set (Magnusson *et al.* 1996) used in this paper consists of 93 lightcurves. The great majority were taken during 1993–94, but seven were from 1969 and two from 1983. Solar phase angles ranged from 10.9° to 60.5°. Of these we judged thirty to provide reliable absolute photometry while for the remainder we allowed a calibration offset. The total number of optical data used was 5208.

The long time base of the optical data set allows for precise calculation of the sidereal spin period P. Magnusson *et al.* (1996) applied various techniques to determine P, the pole direction and an ellipsoidal shape model. They found P = 5.22332640 hr and pole direction $\lambda = 56^{\circ}$, $\beta = -47^{\circ}$. They modeled the shape of Geographos as a biaxial ellipsoid with elongation 2.58. They also investigated possible perturbations of the model that could account for the unequal lightcurve extrema.

The radar data set (Ostro *et al.* 1996) was collected at Goldstone between Aug. 28 and Sep. 2, 1994. The highest resolution imaging was conducted on Aug. 30, 31 and achieved resolutions of 75 m in delay and 87 m in Doppler. Pole solutions from the optical data suggested that the radar would stay very close to the asteroid's equator throughout the entire experiment. The radar images verified this geometry as the image sequence was essentially unchanged from day to day in spite of considerable plane of sky motion between dates. Because of this redundancy and the fact that the Aug. 30 data were stronger, we have used only the Aug. 30 data in our modeling.

DELAY-DOPPLER IMAGING

Because understanding the delay-Doppler imaging geometry is essential to understanding the limitations of the Geographos data set, we here give a brief overview of it. With reference to Fig. 1, the (x,y,z) "body coordinates" are fixed on the asteroid with the z axis corresponding to the spin vector. The (x_r,y_r,z_r) "radar coordinates" are oriented such that the radar lies on the x_r axis and the z_r axis is the projection of the spin vector on the plane of sky.

The radar looks down the x_r axis and sees something like that shown in Fig. 2. Contours of constant delay (constant x_r) are analogous to elevation contours on a topographic map. Iso-Doppler contours are lines parallel to the projected spin vector (constant y_r). Intersections between an iso-delay and iso-Doppler contour define a delay-Doppler resolution cell. It is often the case that these contours will intersect at two or more different points. Scattered energy from all these points will contribute to the corresponding pixel in a delay-Doppler image. This many-to-one mapping is referred to as the "north-south ambiguity" (NSA), and it complicates the interpretation of delay-Doppler images.

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Given sufficient geometric diversity it is often possible to resolve the NSA with a sequence of images.

The radar and asteroid coordinates are related by

 $x_r = (x\cos\psi - y\sin\psi)\cos\delta + z\sin\delta$

 $y_r = x \sin \psi + y \cos \psi$

 $z_r = -(x\cos\psi - y\sin\psi) + z\cos\delta$

where δ is the subradar latitude and ψ is the rotation phase. If $\delta \neq 0$ there is a one-to-one relation between

a given point (x,y,z) and its delay-Doppler trajectory, that is, no other point has the same values of x_r and

 y_r as ψ varies over some interval. Two points that are ambiguous in one image will not be in subsequent

images. A rough analogy can be made between a delay-Doppler image sequence and a set of linearly

independent equations. Although the value of an individual unknown cannot be determined from any

single equation, the leverage afforded by the complete set of equations allows one to uniquely solve for

every unknown.

However, the uniqueness of delay-Doppler trajectories breaks down when $\delta = 0$, because any points

with the same x and y values will always have the same x_r and y_r values and consequently always fall into

the same delay-Doppler pixel. This is analogous to having a set of equations that are linearly dependent; it

is no longer possible to solve uniquely for each unknown. During the Geographos radar experiment the

asteroid's pole was oriented essentially perpendicular to the object's motion on the sky. So, even though

the asteroid moved several tens of degrees on the sky, δ remained essentially zero throughout the

experiment.

Note that even when delay-Doppler trajectories are not unique, the delay-Doppler images still contain

photometric information about the slopes of surface facets. However, this differential shape information

available from image shading is not as strong as the purely geometric leverage resulting from unique

delay-Doppler trajectories.

To explore the effects of an equatorial view on radar-based shape reconstruction, we used a laser radar

system (Andrews et al. 1995) to produce optical "delay-Doppler" images of a scale model clay "asteroid"

with $\delta = 0$ geometry. The fractional resolution and signal-to-noise of the laboratory images were set to be

similar to the Geographos radar data set. A physical model was produced from this laboratory data in the same manner as used to develop the Geographos model described below. Comparison of this model with the known shape serves as a type of "calibration" for the Geographos results and can give us an idea of the types of distortions that might be present in the Geographos model.

Figure 3 shows "observed" and modeled optical "delay-Doppler" images. The model has accounted for the appearance of the delay-Doppler image, but, as Fig. 4 shows, this does not mean that the shapes of the clay model and the computer reconstruction are as close. In fact, to a considerable extent, the reconstruction has "symmetrized" the actual shape along the spin vector (up/down) direction. Features in the model, such as bends and concavities, correspond to real features on the object, but are typically distorted and/or distributed ambiguously between north and south.

We see that a reconstruction in the $\delta = 0$ case can give us an indication of the presence and type of surface features, but cannot constrain their morphology or north/south (N/S) location(s) uniquely. It is also clear that if the actual shape is not N/S symmetric, then the symmetrization of the model will tend to lead to an over estimation of the extents along the spin vector direction and consequently also the volume and surface area. Given that our modeling also treats the radar and photometric properties as free parameters this most likely will lead to a systematic underestimation of albedo.

MODELING

Our physical model of Geographos parameterizes shape, photometric properties (both optical and radar), and spin state. The shape is described by a collection of 1020 triangular facets defined by the locations of 512 vertices. Vertex locations were defined with respect to a point on a reference ellipsoid and were free to move in the direction of the ellipsoid's surface normal at the reference point. Consequently the model represents a deformed ellipsoid. We arrived at the final number of facets by adding vertices during the modeling process until further additions did not lead to a significantly improved fit.

The optical properties of the surface were modeled using a homogeneous, five parameter Hapke photometric function with a single-parameter Henyey-Greenstein particle phase function (Hapke 1993,

eqn. 12.55), as was used to model lightcurves of Gaspra (Simonelli *et al.* 1995), Ida (Simonelli *et al.* 1996), Castalia (Hudson *et al.* 1997), and Toutatis (Hudson and Ostro 1998). The solar phase angle in the optical data set never went below 10° , and the fits displayed little sensitivity to the opposition surge parameters h and B₀, so we fixed these at the "average S-class asteroid" values of h = 0.02, $B_0 = 1.32$ (Helfenstein *et al.* 1996).

Our model radar scattering function has the form $\rho \cos^n \theta$. Here ρ is the normal reflectivity (related to albedo) and n is a measure of the angular width of the scattering pattern. Typically a large value of n corresponds to a surface that is smooth at the scale of an image resolution cell while a small value of n corresponds to a rough surface. (A Lambertian surface has n=2.)

Tentatively, the spin state was assumed to be that of a uniform-density body in principal axis rotation about the axis of maximum moment of inertia. We used the spin state of Magnusson et al. (1996) for our initial conditions. We were prepared to relax this constraint and admit a non-principal-axis spin state and/or density inhomogeneities if our original assumption was not supported by the data.

As the optical data set has a much longer time base than the radar data set, it provides the most leverage for estimating the spin state. Hence, we began modeling by fitting a biaxial ellipsoid to the optical data and solving for the axes, the spin state, and Hapke parameters. Then we approximated that ellipsoid with a triangular-facet polyhedron. Because we were interested to see the extent to which the optical data could resolve the NSA, we used the following procedure. We froze the spin state and fit the shape to the radar data alone. At this point the optical data were included in the modeling, allowing us to see the changes required to the model by the addition of those data. These changes were observable although not very great. Given the probability that the radar-only model suffered from the types of distortions evident in the laboratory experiment, this implies that the optical data did not provide a great deal of leverage to resolve the NSA. Indeed, the subearth latitudes sampled by the lightcurves never extend far into the north or south, but remain within a few tens of degrees of the equator. Nonetheless, as discussed below, there is evidence that the complete data set has some sensitivity to the N/S position of surface features.

Figure 5 shows the observed and modeled radar data corresponding to Aug. 30. Figure 6 shows six of the 93 lightcurve fits. (Plots for all 93 lightcurves are available http://www.eecs.wsu.edu/~hudson/asteroids.html) The top three lightcurves represent a few extremes. The 1969 lightcurve has one of the most northerly subearth latitudes at about 20° and one of the larger phase angles at 53°. The 1983 curve has the smallest phase angle at 11°. The 1994-3-11 curve has one of the more southerly subearth latitudes at -27° and a large phase angle of 50°. The bottom three lightcurves are somewhat representative of the rest of the data set. Generally the model accounts for the asymmetric lightcurve minima but there are cases in which it fails to, as in the 1993-12-13 curve where the deepest observed minimum is about 0.2 mag lower than the modeled minimum. The total rms residual for the entire optical data set was 0.08 magnitude.

Figures 7 and 8 show the shape model. Lines of constant latitude and longitude are drawn at 10° intervals. The views in Fig. 7 are from above the north and south poles while those of Fig. 8 are from within the equatorial plane.

RESULTS

Our model "explains" the observed radar and optical data using a fairly detailed shape model and realistic photometric functions and rotational dynamics. It follows that the model *could be* an accurate representation of Geographos. However, as shown above, there are geometric ambiguities in the data set that probably result in distortion and symmetrization of the shape along the direction of the spin vector. Nonetheless, with the currently available data this model is probably the farthest we can go towards determining the physical properties of Geographos. Consequently we will take it at face value and discuss its implications, keeping in mind that features appearing in the model arise from real features on the object.

Shape

Resolution of the model along directions parallel to the equatorial plane is determined by the ~75 m resolution of the radar images. We conservatively adopt an uncertainty of two pixels or 0.15 km. As illustrated in Fig. 4 the NSA quite likely introduces a large and unknown systematic error for the orthogonal dimension. Keeping this in mind, we adopt 0.15 km as a general uncertainty for distance measurements.

Our shape model has extents along the (long, intermediate, short) axes of inertia of (5.0,2.0,2.1)±0.15 km. The corresponding moments of inertia are (1.0,3.7,3.7)±0.3. The volume is 8.8±1.6 km³, equivalent to a sphere of diameter 2.56 km. A homogeneous ellipsoid with the same volume and moments of inertia would have extents of (4.7,1.9,1.9) km.

The most prominent large-scale feature is the bend near 90° E Longitude. This clearly appears in the delay-Doppler images and was discussed by Ostro *et al.* (1996). Here, in the context of the three-dimensional model we are able to see how this feature explains the different lightcurve minima observed. In Fig. 9 we show the appearance of the model under solar illumination corresponding to the lightcurve extrema M1, m1, M2, m2 of the 1969-3-30 lightcurve (Fig. 6).

The "contact-binary" hypothesis is sometimes offered as an explanation for highly elongated shapes. Because of this, the distribution of mass along the long axis is of interest. Figure 10 plots the cross sectional area normal to the long axis (x axis) as a function of position on that axis. If the density is uniform (as our model assumes) then this is also the mass distribution. There is no bifurcation of mass apparent in this plot. Consequently this result provides no evidence for, although it does not rule out, the possibility that Geographos is a "contact-binary" asteroid, that is, that Geographos formed from two bodies that once were separate.

Surface Features

We identify seven surface features prominent in the delay-Doppler images, which we label C1-7 (Fig. 11), and discuss them in turn. The model is generated with respect to the rectangular body system (x,y,z)

with origin at the center of mass. The z axis is the north pole while the x axis is the axis of minimum inertia pointing more or less in the direction of the 0° rotation phase origin adopted by Ostro et al. (1995). In this paper we will find it convenient to locate points on the surface by latitude (δ) and longitude (α). In Figs. 7, 8, and 11 longitude, latitude grids with 10° spacing have been drawn on the model to aid in this discussion. We define latitude (δ) and East longitude (α) by

$$r = \sqrt{x^2 + y^2 + z^2}$$

(x, y, z) = $r(\sin \delta \cos \alpha, \sin \delta \sin \alpha, \cos \delta)$

while West longitude is given by 360° - α .

In Fig. 11 the seven features are circled. The middle panel shows delay-Doppler images summed over 30° rotation-phase windows and it corresponds to Fig. 11(c) of Ostro *et al.* (1996). Viewing the shape model from above the north/south pole generated the top/bottom panel. The light source was in the equatorial plane and rotated 30° between images. For the top panel the images were flipped left to right to give them the same orientation as the south-pole view that characterizes the delay-Doppler images.

When viewed in this manner the appearance of the model is roughly analogous to a delay-Doppler image. However there are some important differences that should not be forgotten. First, a delay-Doppler image combines the contributions from both the north and south. Second, the relation between surface normal and brightness is different for the two types of images. The model images are viewed at a 90° phase angle while the radar viewed the asteroid at 0° phase, so surface facets near the leading edge contribute significantly more energy to the delay-Doppler image than to the optical image. In short, there is no optical imaging geometry that precisely corresponds to the delay-Doppler imaging geometry. We have adjusted for this effect somewhat by applying a nonlinear brightness filter to the model images. Still, it must not be assumed that the model when viewed in this manner is supposed to accurately predict the delay-Doppler images. To do that, the correct delay-Doppler imaging geometry must be employed, as it is during the modeling process (Fig. 5). However, Fig. 11 does allow us to see what regions of the surface were unilluminated by the radar.

By viewing the model in this manner, we are able to see if it tends to place a feature in the north or south. For example, features C1 and C2 are responsible for the "knobish," almost detached appearance of the 0° end. Figure 11 suggests that concavities located in the south are primarily responsible for these features. C1 is located near (5°S,10°W) while C2 is near (10°S,20°E).

Features C3, C4, and C5 are the features most suggestive of craters in the delay-Doppler images. The model prefers a southern location for C3 (40°S,20°W) and northern locations for C4 (90°N) and C5 (20°N,180°W).

C6 is the feature responsible for the pinwheel-like appearance of the 180°W end. The model places a concavity in the north at (10°N,170°E) to explain this.

C7 is an elongated feature that could possibly be two close craters. The model explains this by a concavity near (40°S,130°E).

Optical and Radar Scattering Properties

The radar scattering law has the form $\rho \cos^n \theta$ where ρ is normal reflectivity and n is a measure of the angular width of the scattering. If the surface scattering is modeled as specular reflection from a distribution of surface facets, then $\theta = \tan^{-1} \sqrt{2/n}$ is the rms surface slope and $R = 2\rho/(n+2)$ is the Fresnel reflection coefficient.

Our model gives $n = 1.72\pm0.5$ and $\rho \ge 0.17$ where we take the ρ solution as a lower bound in keeping with our assumption that the projected area of the model is likely to be larger than that of the asteroid. The value of n suggests more diffuse scattering than found for either Toutatis (n = 2.3) or Castalia (n = 2.8). The equivalent spherical albedo of Geographos is ≥ 0.12 . For comparison Castalia's value is 0.16 and for Toutatis it is 0.21.

For the three Hapke parameters that we solved for, we found $w \ge 0.22$, $g = -0.34 \pm 0.1$, and $\overline{\theta} = 25 \pm 10^{\circ}$. Where as for ρ we take the model's w value as a lower bound on the single-scattering albedo. Uncertainties for g and $\overline{\theta}$ were derived through covariance calculations and a consideration of possible

systematic errors due to the NSA. These values are quite close to those found for Dactyl, w = 0.21, g = -0.33, and $\overline{\theta} = 23^{\circ}$, for which opposition surge parameters h = 0.2 and $B_0 = 1.53$ were assumed (Helfenstein *et al.* 1996).

Spin State

Our spin state solution differs negligibly from that of Magnusson *et al.* (1996). This makes sense as we are using the same optical data and the optical data are what primarily constrain the spin state in this case. We found $\lambda = 55 \pm 4^{\circ}$, $\beta = -46 \pm 6^{\circ}$, and $P = 5.2233270 \pm 0.00000072$ hr where we have retained the uncertainties of Magnusson *et al.*

It has been suggested that subtle periodicities in the lightcurves provide evidence of non-principal-axis rotation and one or more companion satellites (Prokof'eva *et al.* 1997). We tested the non-principal-axis rotation hypothesis by freeing the spin state from the principal-axis, uniform-density constraints placed on it during most of the modeling, but found no significant evidence for non-principal-axis rotation.

IMPLICATIONS

Our shape model is distinguished by its elongation, a major central indentation, circular concavities that most likely are impact craters with diameters of several hundred meters, other topographic relief that may or may not be impact craters, and unusual structure at the ends. How should these characteristics be understood? Ostro *et al.* (1996) surmised that "Geographos presumably is the cumulative product of a sequence of collisions, perhaps originating in disruption of a very much larger parent body and proceeding through an interval of relatively low-energy impacts." Richardson et al. (1998) have presented simulations that demonstrate the possibility that Geographos' shape has been resculpted by tidal distortion of a rubble pile during a close Earth encounter (see also Solem and Hills 1996). Simulations by Scheeres *et al.* (1996, 1998) and Asphaug *et al.* (1998) demonstrate the complexity of the distribution of impact ejecta for small, irregularly shaped bodies and the dependence of the outcome of cratering events on the target's pre-existing internal structure.

There probably are numerous, very different scenarios that could offer plausible qualitative explanations for this asteroid's detailed characteristics. For example, the unusual morphology of Geographos' ends may involve the systematics of ejecta removal and deposition caused by the combination of the asteroid's gravity field and rotation (Ostro *et al.* 1996), but other viable possibilities include tidal distortion, collisional spallation, and simply impact carving. Simulations using our model may elucidate these possibilities.

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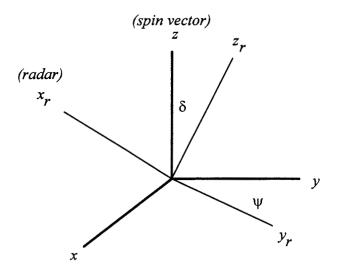


Fig. 1. Relation between asteroid and radar coordinates. Angles δ and ψ are the subradar latitude and rotation phase, respectively.

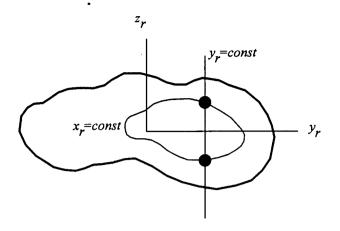


Fig. 2. Plane of sky appearance of asteroid and iso-delay (x_r =const) and iso-Doppler (y_r =const) contours.

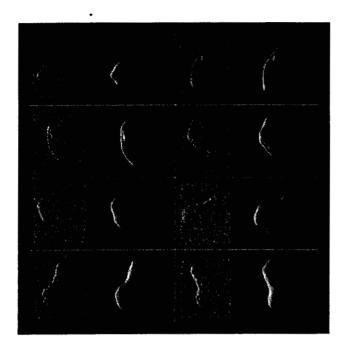


Fig. 3. Observed (first and third columns) and modeled (second and fourth columns) optical-radar images of clay model asteroid. Fractional resolution and signal-to-noise ratio is similar to Goldstone Geographos radar data set.

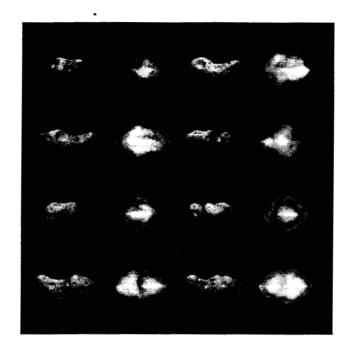


Fig. 4. True shape (first and third columns) and modeled shape (second and fourth columns) of clay asteroid model. Spin vector is up.

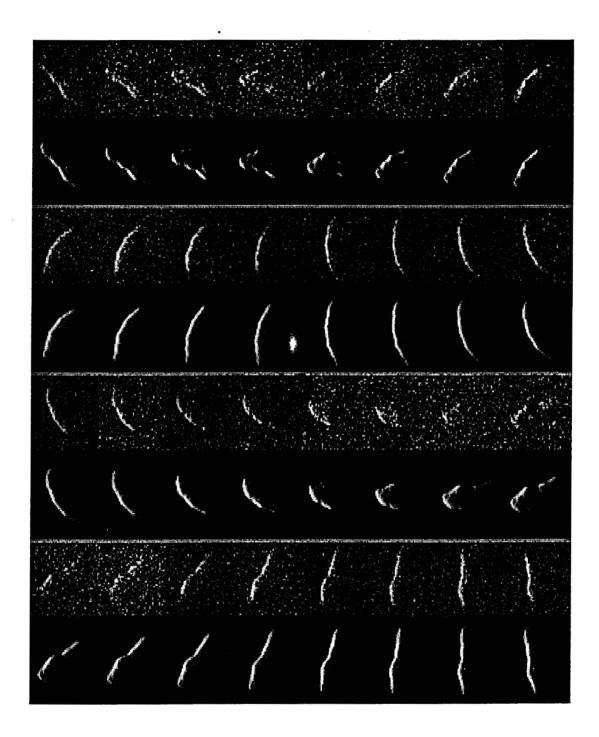


Fig. 5. Geographos delay-Doppler radar images. In each of the four sections the top row shows observed data and the row below shows the corresponding modeled data. Time increases from left to right and top to bottom. Delay increases from top to bottom and Doppler from left to right.

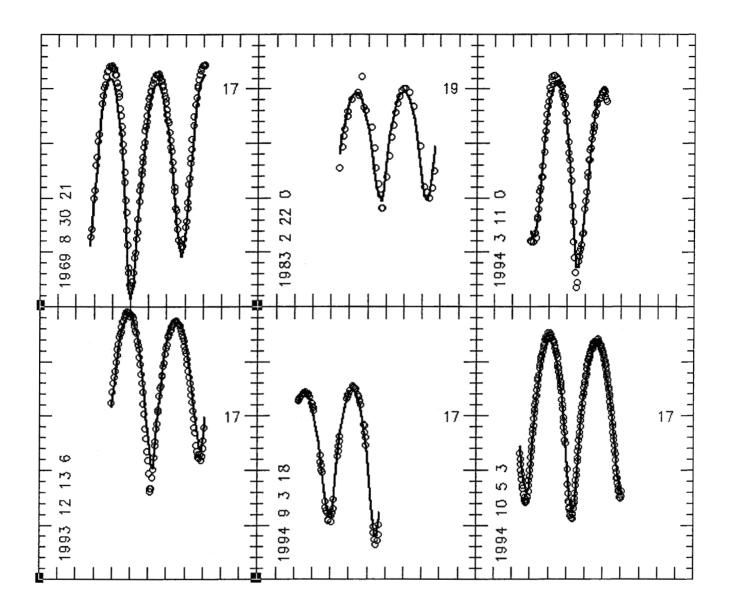


Fig. 6. Selected lightcurve fits. Vertical ticks are at 0.1 magnitude spacing. Horizontal ticks are at 1 hr spacing. Vertical labels give UTC (year mn dd hh) at start of plot. Five of the lightcurves provided absolute photometry and one of the vertical ticks is labeled as a reference (magnitude of either 17 or 19) while the other (top right) gives relative photometry only.

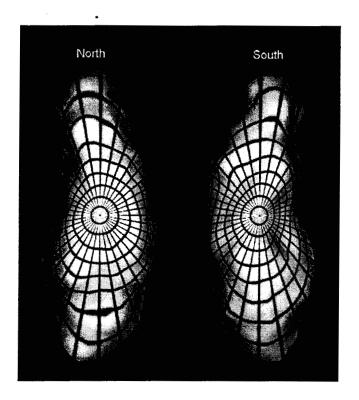


Fig. 7. View of the model from above north pole (left) and south pole (right). Contours of constant longitude and latitude are drawn at 10° intervals. 0° longitude is up.

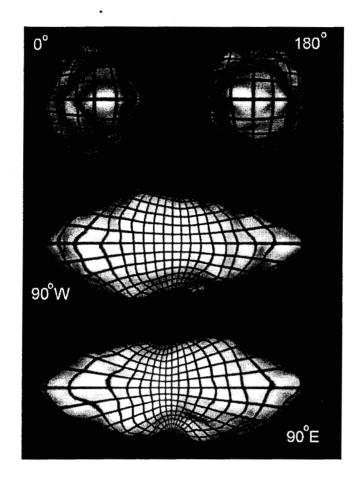


Fig. 8. Views of model from within equatorial plane. Longitudes are: top left 0°, top right 180°, middle 90° W, bottom 90° E.

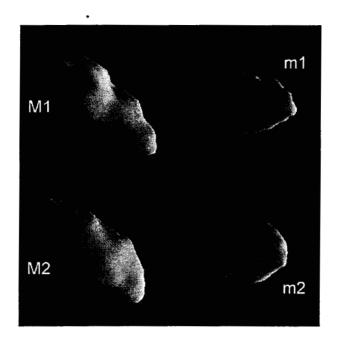


Fig. 9. Model viewed with solar illumination at times corresponding to extrema of 1969-3-30 lightcurve

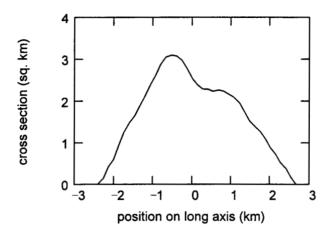


Fig. 10. Distribution of volume on long axis.

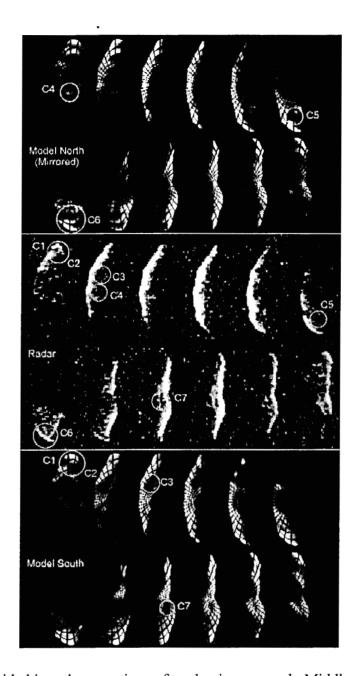


Fig. 11. Figure is divided into three sections of twelve images each. Middle section: Fig. 11 from Ostro *et al.* (1996) showing delay-Doppler images averaged over 30° rotation phase windows. The geometry corresponds to a view from above the south pole. Top section: Geographos model viewed from above the north pole with equatorial illumination varying in 30° increments. Each of the twelve images has been mirror imaged left-right to correspond to the geometry of the

delay-Doppler images. Bottom section: Geographos model viewed from above the south pole with equatorial illumination varying in 30° increments.